

Artificial gorilla troops optimization algorithm for key term separated input non-linear output error system identification

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ABSTRACT

This research study gives an overview of the identification of an input non-linear output error system (IN-OES) leveraging an artificial gorilla troops optimization algorithm (AGTOA). The key term, separated identification auxiliary-based model IN-OES, with the heuristic optimization algorithm AGTOA, is implemented to predict the parameters of the system. The efficiency of the swarm-inspired algorithm AGTOA is exploited for the parameter prediction of the IN-OES system, and promising outcomes were observed through the evaluation of fast convergence, prediction of real parameters of the system, and high fitness values, such as best fitness values, average fitness values, worst fitness values, and standard deviation values in no-noise and multiple-noise scenarios, i.e., 0, 0.00021, 0.0022, 0.023.

Keywords: Non-linear systems; input non-linear output error system; optimization algorithm; artificial gorilla troops optimization algorithm; heuristic technique.

1. INTRODUCTION

Nonlinear systems [1-3] are intricately interconnected because of their impulsive behavior, sensitivity to primary conditions, and that the response does not follow a simple linear pattern; that is to say, the fact that their operation is not predictable [4-5]. It is this complexity that makes non-linear systems the most realistic models of many natural [6] and engineered processes [7-8]. These systems are typically applicable in various aspects such as artificial intelligence [9-10], artificial neural networks [11-12], machine learning [13-15], recommender systems [16-17], cloud computing [18-19], intelligent computing algorithms [20-22], and many more.

One commonly studied class of nonlinear systems is the input non-linear output error system (IN-OES) [23]. These models are particularly important in system identification and control [24-25], where precisely predicting system performance is crucial for optimization and performance improvement.

The Input Nonlinear Output Error System (IN-OES) model combines both static and dynamic mechanisms to capture the non-linear characteristics of a system. To accurately identify the parameters of IN-OES models, optimization techniques [31-32]

are often required. These techniques can be generally characterized into local [33-34] and global search algorithms [35-37]. Local search algorithms such as the least mean square algorithm [38-39], fractional gradient algorithm [40-41], and local beam search algorithm [42], focus on releasing a single solution through iterative improvement. While they offer faster convergence, they are likely to get stuck in local optima. On the other hand, global search algorithms [43] are designed to explore the entire solution space, thereby mitigating the risk of local optima entrapment. Popular global optimization techniques include the particle swarm optimization algorithm [44-45], the genetic algorithm [46-47], the cuckoo-search algorithm [48-49], and the improved shuffled frog leaping algorithm [50].

A recently developed global optimization algorithm, the Artificial Gorilla Troops Optimization Algorithm (AGTOA) [51], draws motivation from the collective intelligence and social behaviors of gorilla troops. This heuristic algorithm balances exploration and exploitation by impersonating the natural foraging, movement, and survival approaches of gorillas. It is mainly well suited for solving complex optimization problems such as parameter identification in IN-OES models.

The significant parts of the study are as follows

- The Artificial Gorilla Troops Optimization Algorithm (AGTOA) is applied for the identification of the input non-linear output error system (IN-OES).
- A fitness function based on minimizing the mean square error is formulated to reduce the gap between the predicted response and the actual response in the IN-OES model.
- An auxiliary model combined with the key term is utilized to manage the indeterminate and cross-product terms within the IN-OES structure, simplifying the identification process.
- The performance is evaluated based on parameter estimation accuracy, learning curve, i.e., convergence speed, and consistent results in identifying actual parameters.

A graphical picture of the proposed methodology is provided

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in Figure 1. The structure of the input non-linear output error system (IN-OES) is provided in Section 2. The working principles of the AGTOA are discussed in section 3, and the analysis, results, and conclusion are provided in sections 4 and 5, respectively.

2. INPUT NON-LINEAR OUTPUT ERROR SYSTEMS (IN-OES)

Input non-linear output error system (INO-ES) [52] is represented in Figure 2 and numerically shown in Equation (1) [53]

$$X(i) = \frac{c(j)}{d(j)} \ddot{k}(i) + \theta(i), \quad (1)$$

where, $X(i)$ presents the outcome of the system, $\frac{c(j)}{d(j)}$ shows polynomial operators, $\ddot{k}(i)$ shows the non-linear outcome and shows noise. The noise-free portion of IN-OES is represented in Equation (2) [53]

$$\tau(i) = \frac{c(j)}{d(j)} \ddot{k}(i), \quad (2)$$

The resultant equation of the mathematical model of the IN-OES is shown in Equation (3) [53]

$$Z(i) = \rho^T(i)X + \theta(i). \quad (3)$$

where, $Z(i)$ is the resultant vector, ρ^T shows the transposition of parameters and X shows the information vector.

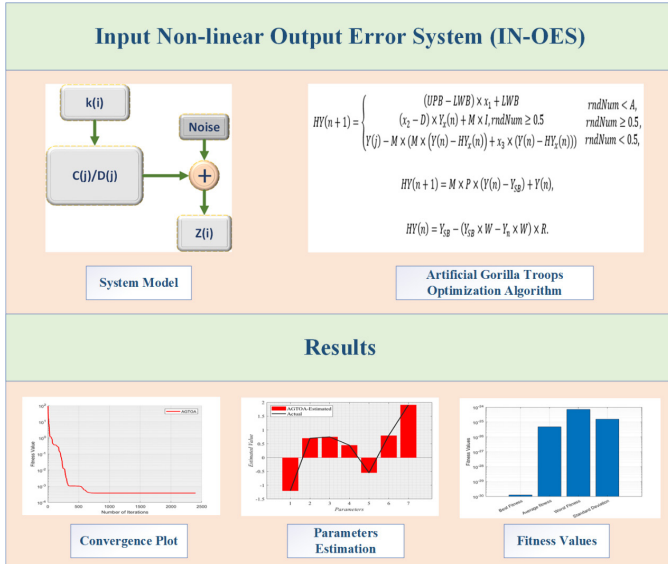


Fig. 1 Graphical representation of the study

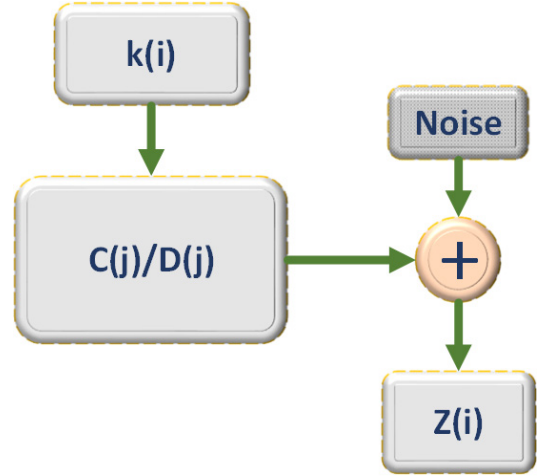


Fig. 2 Input non-linear output error systems (IN-OES) model's visual representation

3. ARTIFICIAL GORILLA TROOPS OPTIMIZATION ALGORITHM (AGTOA)

The Artificial Gorilla Troops Optimization Algorithm (AGTOA) [51] takes inspiration from the shared intellect and societal activities of gorilla troops. This algorithm balances exploration and exploitation by mimicking the natural foraging, movement, and survival approaches of gorillas [54]. The update rules of the AGTOA are shown in Equations 4, 5, and 6.

$$HY(n+1) = \begin{cases} (UPB - LWB) \times x_1 + LWB & \text{randNum} < A, \\ (x_2 - D) \times Y_s(n) + M \times I, \text{randNum} \geq 0.5 & \text{randNum} \geq 0.5, \\ Y(j) - M \times (M \times (Y(n) - HY_s(n)) + x_3 \times (Y(n) - HY_s(n))) & \text{randNum} < 0.5, \end{cases} \quad (4)$$

$$HY(n+1) = M \times P \times (Y(n) - Y_{SB}) + Y(n), \quad (5)$$

$$HY(n) = Y_{SB} - (Y_{SB} \times W - Y_n \times W) \times R. \quad (6)$$

4. RESULTS AND DISCUSSIONS

The results of the study for identifying the parameters of the input non-linear output error system (IN-OES) are presented in this section. The simulations are executed on 2400 number of iterations with 24 independent runs and 75 population size. The results are executed on the MATLAB tool with system specifications of Intel Core i-5 12th generation with 24 GB of RAM. The results are shown in table and figure form, showcasing the robustness of the artificial gorilla troops optimization algorithm (AGTO) for the IN-OES model. Table 1 shows the accuracy achieved by the AGTO in multiple noise levels, such as .0, 0.00021, 0.0022, 0.023. From Table 1, we can say that the AGTOA achieved high accuracy with no noise, and accuracy becomes low as we increase the noise level. table 1 shows the best fitness value, average fitness value, standard deviation value, and worst fitness value. The parameters of the system are taken from [55].

Table 1 Best-fitness (B.F), Average-fitness (A.F), and Worst-fitness (W.F) of AGTO

Algorithm	Noise level	B.F	A.F	W.F	S.T.D
AGTOA	.0	1.2942E-30	4.8623E-26	7.1733E-25	1.5734E-25
	0.00021	4.2028E-08	4.2028E-08	4.2028E-08	3.5513E-17
	0.0022	6.1374E-06	6.1374E-06	6.1374E-06	6.0145E-16
	0.023	3.8209E-04	3.8209E-04	3.8209E-04	5.3807E-15

The learning curves represented in Figure 3 show the convergence speed of the AGTO, how quickly and consistently it converges to achieve the highest accuracy, and how well it performs in different noise scenarios, i.e., .0, 0.00021, 0.0022, 0.023. From Table 1, we can clearly state that with no noise, the AGTOA gives a fitness of 1.2942E-30, and as we implemented the noise and increased it, the fitness values decreased, such as for the noise cap theta equals, .00021, 0.0022, 0.023, the best fitness values are 4.2028E-08, 6.1374E-06, and 3.8209E-04.

Table 2 and Figure 4 show that the AGTOA performed exceptionally well at identifying the parameters of the input non-linear output error system (IN-OES). By increasing the noise, the performance of the algorithm gets low, but it still accurately predicts the system parameters. From these results, we can say that the AGTOA performance is well enough to identify the parameters of IN-OES.

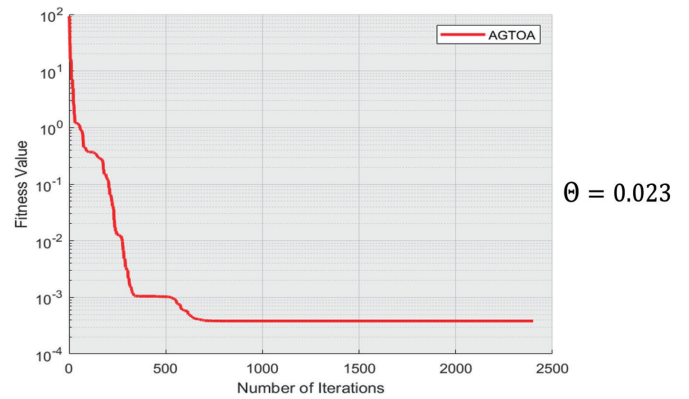
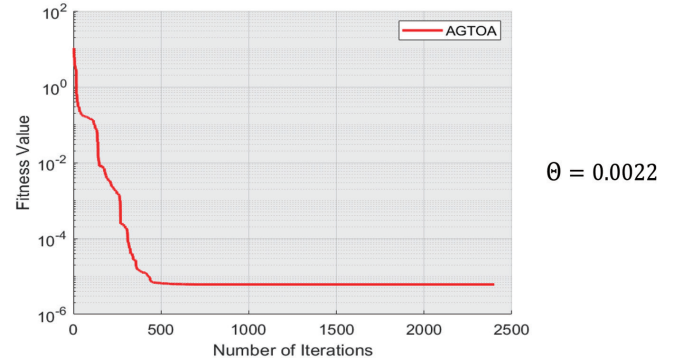
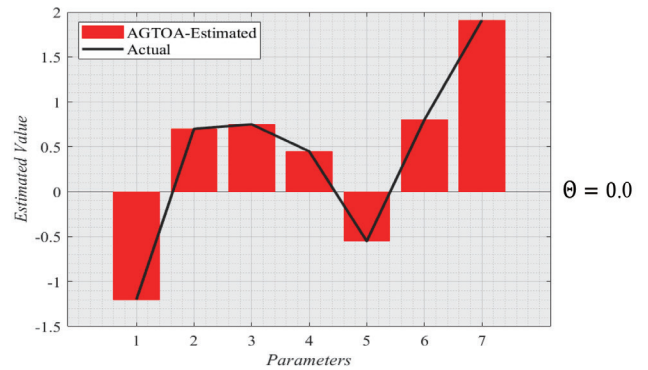
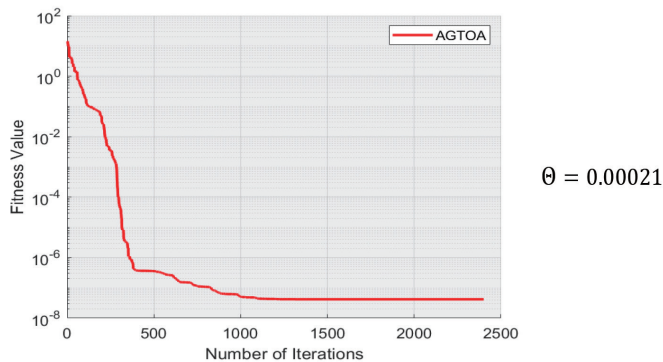
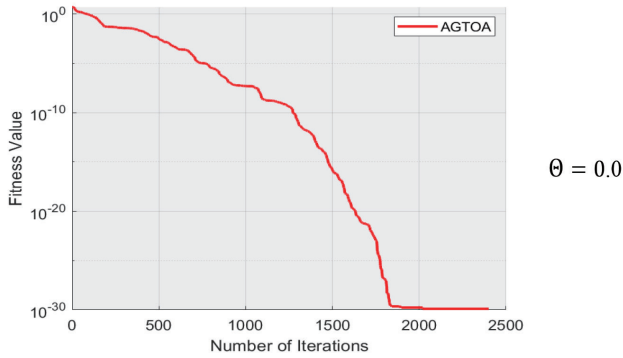


Fig. 3 Learning curves of AGTOA



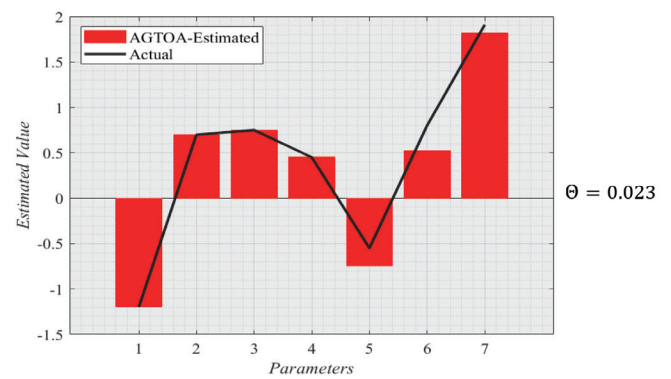
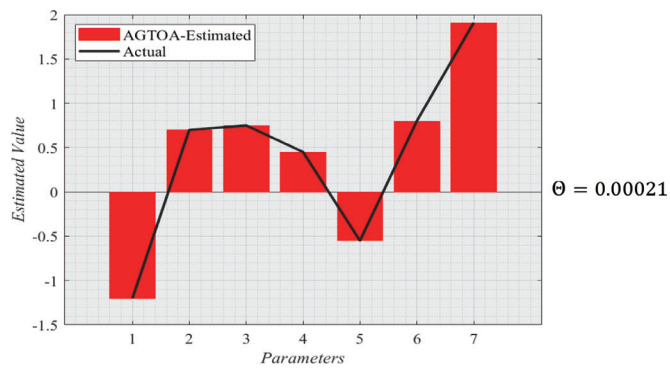


Fig. 4 Parameter's estimation of AGTOA

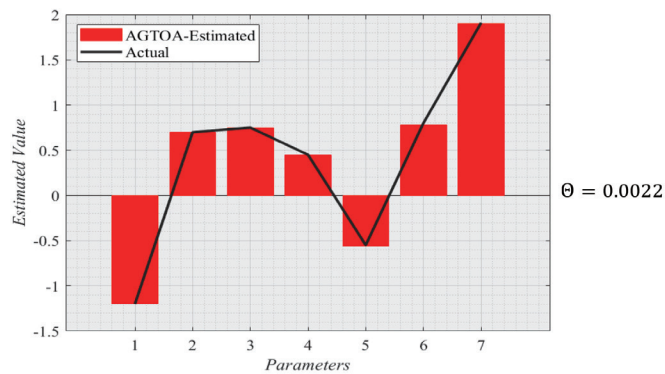
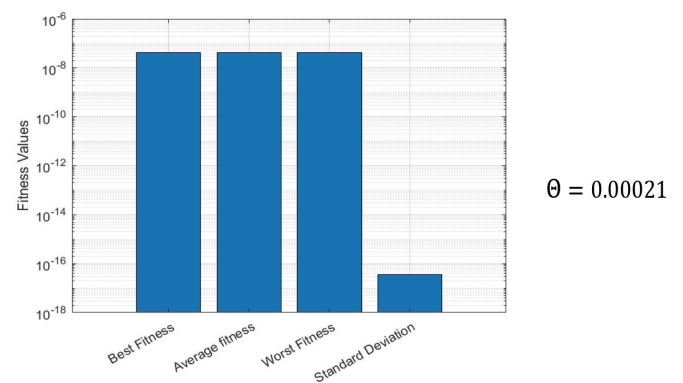
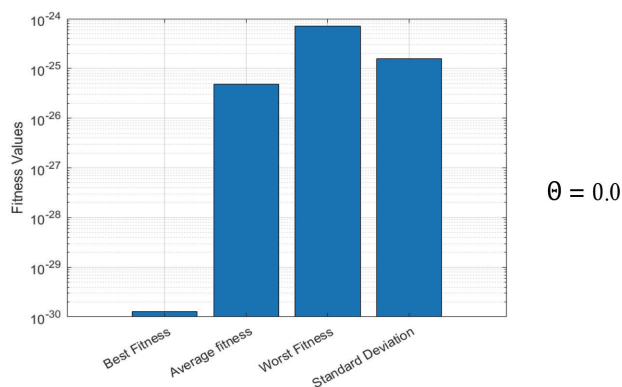


Table 2 Weight approximation of AGTOA

Algorithm	Noise level	P.1	P.2	P.3	P.4	P.5	P.6	P.7
AGTOA	.0	-1.200	0.700	0.750	0.450	-0.550	0.800	1.910
		-1.200	0.700	0.750	0.450	-0.552	0.797	1.909
		-1.200	0.700	0.750	0.450	-0.560	0.780	1.901
		-1.198	0.698	0.748	0.452	-0.747	0.524	1.820
Actual Parameters		-1.2	0.7	0.75	0.45	-0.55	0.8	1.91

Figure 5 shows the best, average, and worst fitness values, and standard deviation bar plots showcasing how the AGTOA performs in different noisy and no-noise scenarios, i.e., .0, 0.00021, 0.0022, 0.023. The plots show that AGTOA performs well in all noisy and no-noise scenarios.



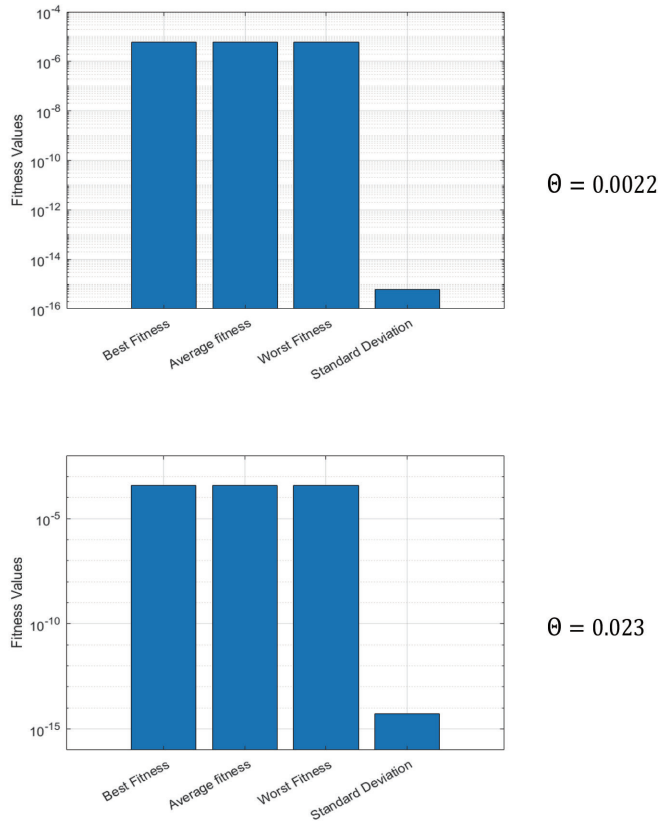


Fig. 5 Fitness values of AGTOA

5. Conclusion

In this research study, for the input non-linear output error system (IN-OES), the heuristic optimization algorithm, artificial gorilla troops optimization algorithm (AGTOA) is exploited. The results show that the AGTOA gives promising outcomes in terms of fast convergence and high fitness values, such as best fitness values, average fitness values, worst fitness values, and standard deviation values. AGTOA predicts the parameters of the system in no-noise and multiple-noise scenarios, such as .0, 0.00021, 0.0022, 0.023. By increasing the noise, a slight variation in predicting the original parameters is observed, but it is still considered to be a very well-performing algorithm on that system and gives expected outcomes. In future work, fractional calculus on the system model INO-ES or algorithm AGTOA can be implemented with different nonlinearities such as geometry, material, and contact nonlinearities, or different noise types such as asymmetric noise, Gaussian noise, etc.

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